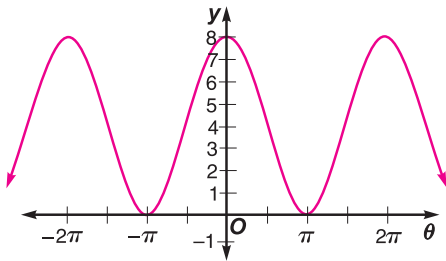


## Practice

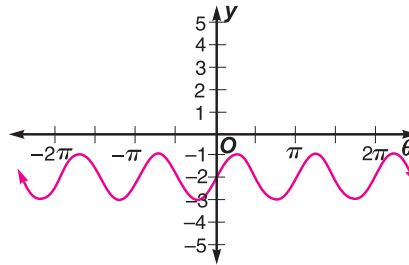
## Translations of Sine and Cosine Functions

State the vertical shift and the equation of the midline for each function. Then graph each function.

1.  $y = 4 \cos \theta + 4$

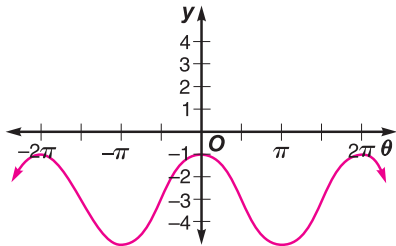
4 units up;  $y = 4$ 

2.  $y = \sin 2\theta - 2$

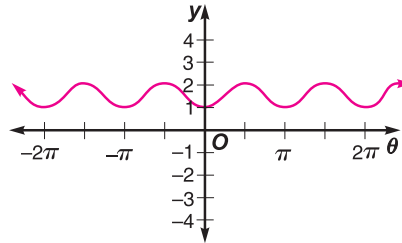
2 units down;  $y = -2$ 

State the amplitude, period, phase shift, and vertical shift for each function. Then graph the function.

3.  $y = 2 \sin \left( \theta + \frac{\pi}{2} \right) - 3$

2;  $2\pi$ ;  $-\frac{\pi}{2}$ ; -3

4.  $y = \frac{1}{2} \cos (2\theta - \pi) + 2$

 $\frac{1}{2}$ ;  $\pi$ ;  $\frac{\pi}{2}$ ; 2

Write an equation of the specified function with each amplitude, period, phase shift, and vertical shift.

5. sine function: amplitude = 15, period =  $4\pi$ , phase shift =  $\frac{\pi}{2}$ , vertical shift = -10

$$y = \pm 15 \sin \left( \frac{\theta}{2} - \frac{\pi}{4} \right) - 10$$

6. cosine function: amplitude =  $\frac{2}{3}$ , period =  $\frac{\pi}{3}$ , phase shift =  $-\frac{\pi}{3}$ , vertical shift = 5

$$y = \pm \frac{2}{3} \cos (6\theta + 2\pi) + 5$$

7. sine function: amplitude = 6, period =  $\pi$ , phase shift = 0, vertical shift =  $-\frac{3}{2}$

$$y = \pm 6 \sin 2\theta - \frac{3}{2}$$

## Translating

In Lesson 6-4, we saw how to affect the graph of a sine or cosine function by translating it. These results are summarized in the following theorem.

## Example 1

## Example 2

Step 1

Step 2

Step 3

Step 4

## Sketch the

1.  $y = 3 \sin \theta$

2.  $y + 5 = \cos \theta$

## Graph one

3.  $y = 6 \cos \theta$

4.  $y = 6 \cos \theta$