

3.2.14 Solving Equations with Variables on Both Sides with Distributing and Combining

A rock-climbing gym charges nonmembers \$16 per day to use the gym and \$8 per day for equipment rental. Members pay a yearly fee of \$450 for unlimited climbing and \$6 per day for equipment rental. Write and solve an equation to find the number of days you must use the gym to pay the same amount.

Equation: $16d + 8d = 450 + 6d$

Solve the equation:

$$\begin{array}{r} 24d = 450 + 6d \\ -6d \quad -6d \\ \hline 18d = 450 \\ \frac{18}{18} \quad \frac{450}{18} \\ d = 25 \end{array}$$

Explain your solution

in context: Members & nonmembers pay the same in 25 days.

$$7(-2k + 4) - 6 = 7k - 20$$

$$\begin{array}{r} -14k + 28 - 6 = 7k - 20 \\ -14k + 22 = 7k - 20 \\ +14k \quad +14k \\ \hline 22 = 21k - 20 \\ +20 \quad +20 \\ \hline 42 = 21k \\ \frac{42}{21} = \frac{21k}{21} \\ 2 = k \end{array}$$

Solve the following equations for the given variable

$$\begin{array}{r} 24 + 8x = 8(5x + 8) + 8x \\ 24 + 8x = 40x + 64 + 8x \\ 24 + 8x = 48x + 64 \\ -8x \quad -8x \\ \hline 24 = 40x + 64 \\ -64 \quad -64 \\ \hline -40 = 40x \\ \frac{-40}{40} = \frac{40x}{40} \\ -1 = x \end{array}$$

$$-1 = x$$

One container starts with 18 cups of water and water is added to the cup at a rate of 2 cups per minute. Another container starts with 110 cups of water and loses water at a rate of 6 cups per minute. After how many minutes will the two containers have the same amount of water in them?

Equation:

$$18 + 2p = 110 - 6p$$

Solve the equation:

$$\begin{array}{r} 18 + 2p = 110 - 6p \\ -18 \quad -18 \\ \hline 2p = 92 \\ \frac{2p}{2} = \frac{92}{2} \\ p = 46 \end{array}$$

Explain your solution

in context of the problem: They have the same amount of water in 46 minutes.