

## Solving Linear Systems by Elimination/Combinations

$$\begin{array}{r} 5+7 \\ 7+5 \end{array}$$

$$\begin{aligned} 1. \quad x + 3y &= 12 \\ -3y + x &= 30 \end{aligned}$$

$$\begin{array}{r} x + 3y = 12 \\ x - 3y = 30 \\ \hline 2x = 42 \\ \frac{2x}{2} = \frac{42}{2} \end{array}$$

$$x = 21$$

$$(21, -3)$$

$$\begin{array}{r} 21 + 3y = 12 \\ -21 \quad y - 21 \\ \hline 3y = -9 \\ \frac{3y}{3} = \frac{-9}{3} \quad y = -3 \end{array}$$

1.

2.

3.

$$2. \quad 3x + 2y = 8$$

$$\begin{array}{r} 2y = 12 - 5x \rightarrow 2y = 12 - 5(2) \\ +5x \quad +5x \quad 2y = 12 - 10 \\ 2y = 2 \\ \frac{2y}{2} = \frac{2}{2} \\ y = 1 \end{array}$$

$$\begin{array}{r} (3x + 2y = 8) - 1 \\ 5x + 2y = 12 \\ \hline -3x - 2y = -8 \\ 5x + 2y = 12 \\ \hline 2x = 4 \\ \frac{2x}{2} = \frac{4}{2} \\ x = 2 \end{array}$$

$$(2, 1)$$

$$3. \quad -6x + 3y = -6$$

$$\begin{array}{r} 6y = -2x + 30 \\ +2x \quad +2x \end{array}$$

$$\begin{array}{r} -6x + 3y = -6 \\ 3(2x + 6y = 30) \\ \hline -6x + 3y = -6 \\ 6x + 18y = 90 \\ \hline 21y = 84 \\ \frac{21y}{21} = \frac{84}{21} \\ y = 4 \end{array}$$

$$\begin{array}{r} 6(4) = -2x + 30 \\ 24 = -2x + 30 \\ -30 \quad -30 \\ \hline -6 = -2x \\ \frac{-6}{-2} = \frac{-2x}{-2} \quad x = 3 \end{array}$$

$$(3, 4)$$

$$\begin{array}{r}
 4. \quad y = 2x - 4 \\
 \left\{ \begin{array}{r} 2x - y = 52 \\ -2x + y = -4 \end{array} \right. \\
 \hline
 0 = 48
 \end{array}$$

No solution

$$\begin{array}{r}
 y = 2x - 4 \\
 -y = -2x + 52 \\
 \hline
 0 = 48
 \end{array}$$

$$\begin{array}{r}
 5. \quad 4y = 5 = -7x + 5 \\
 4y = 2x + 14 \\
 -1(4y = -7x + 5) \\
 4y = 2x + 14
 \end{array}$$

$$\begin{array}{r}
 -4y = 7x - 5 \\
 4y = 2x + 14 \\
 \hline
 0 = 9x + 9 \\
 \cdot 9 \quad -9 \\
 \hline
 -9 = 9x \quad x = -1
 \end{array}$$

4.  
5.

$$\begin{array}{r}
 (-1, 3) \\
 4y = 2(-1) + 14 \\
 4y = -2 + 14 \\
 4y = 12 \\
 \cdot 4 \quad /4 \\
 y = 3
 \end{array}$$

## Checklist:

1. Are Like Terms in Columns? ☐
2. Do I have coefficients that are opposites? ☐
3. Solve for one variable ☐
4. Use substitution to solve for the other variable ☐
5. Check you solution ☐

6. The drama club is selling gift baskets to raise money for new costumes. During the fall play, they sold a combined 3 regular gift baskets and 4 deluxe gift baskets, earning a total of \$227. During the spring musical, they sold 6 regular gift baskets and 2 deluxe gift baskets, earning a total of \$208.

a. Identify the variables

x: cost of a regular gift basket

y: cost of a deluxe gift basket

b. Write and solve a system to determine the price of each type of gift basket.

$$\begin{array}{r}
 3x + 4y = 227 \rightarrow 3(21) + 4y = 227 \\
 -2(6x + 2y = 208) \\
 \hline
 3x + 4y = 227 \\
 -12x - 4y = -416 \\
 \hline
 -9x = -189 \\
 \cdot -9 \quad -9 \\
 \hline
 x = 21
 \end{array}$$

$$\begin{array}{r}
 63 + 4y = 227 \\
 -63 \quad -63 \\
 \hline
 4y = 164 \\
 y = 41
 \end{array}$$

c. Explain your solution in the context of the problem.

The regular gift basket sold for \$21 and the deluxe gift basket sold for \$41.